

Online Workshop on Network Science for Fluid Dynamics

24-25, June 2020

Complex networks approach to wall-bounded turbulence

Research group @ Politecnico di Torino (Italy)



Group members:

Dr. Giovanni Iacobello (Speaker)

Prof. Stefania Scarsoglio

Prof. Luca Ridolfi

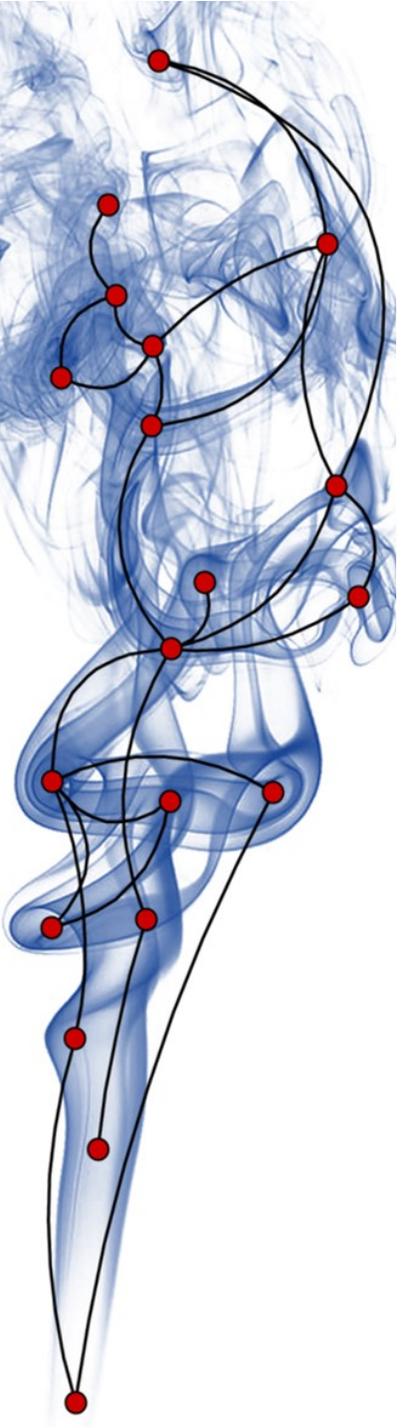
Davide Perrone, PhD student

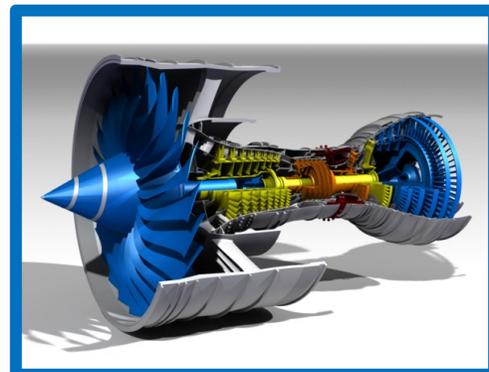
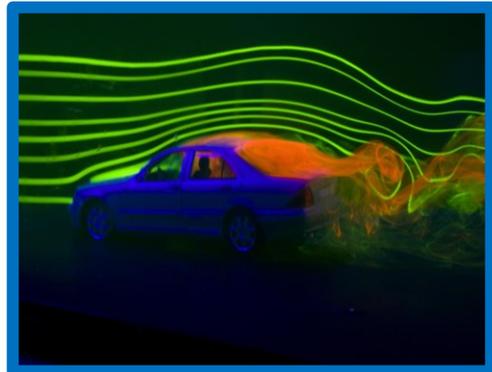
Collaborations:

Prof. J.G.M. Kuerten (TU Eindhoven)

Prof. Pietro Salizzoni (École Centrale de Lyon)

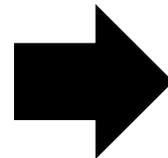
Prof. Umberto Morbiducci (Politecnico di Torino)





Why wall-turbulence?

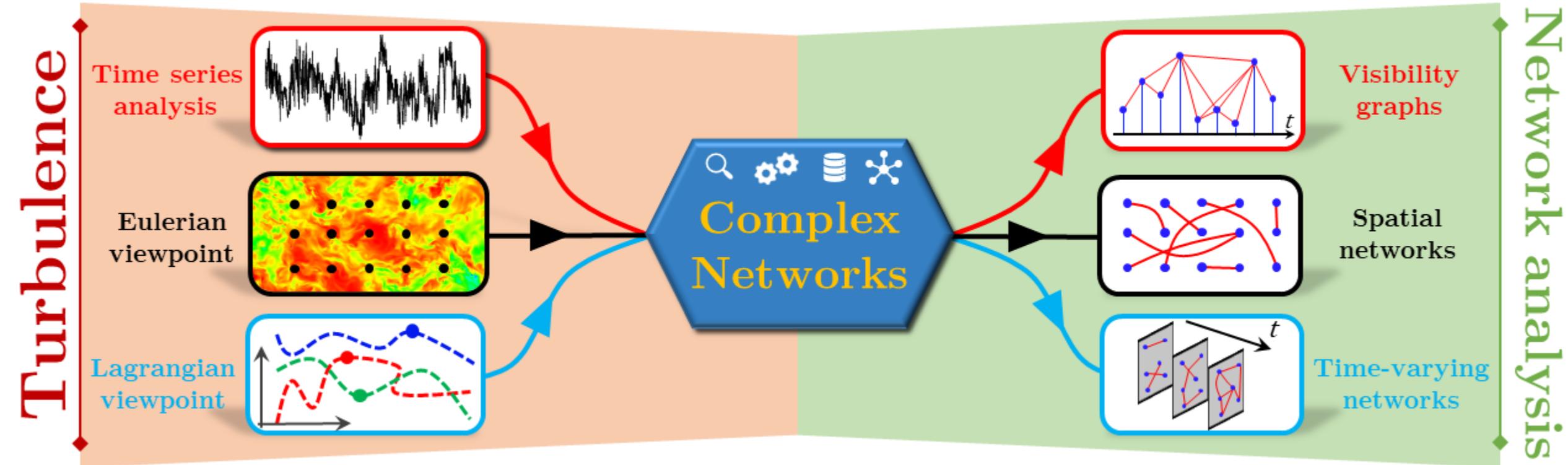
- Technological importance
- Energetics – Optimization
- Fluid transport
- Environmental issues

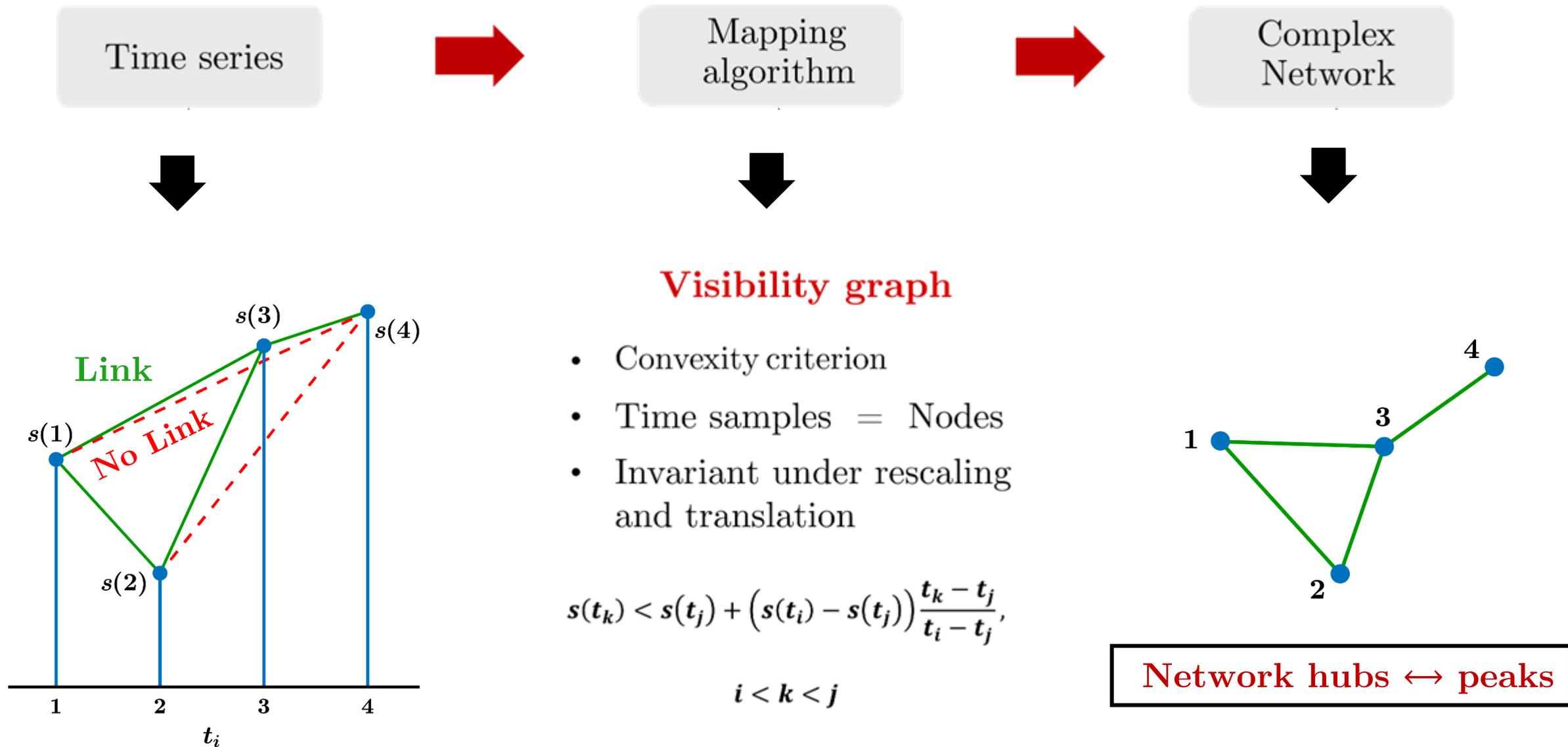


“A **5% reduction** of the transportation energy loss in the US would have an environmental impact comparable to a **doubling** of wind energy production.” *



* Smits A. J. and Marusic I.. “Wall-bounded turbulence”. In: Physics Today 66.9 (2013), pp. 25–30.

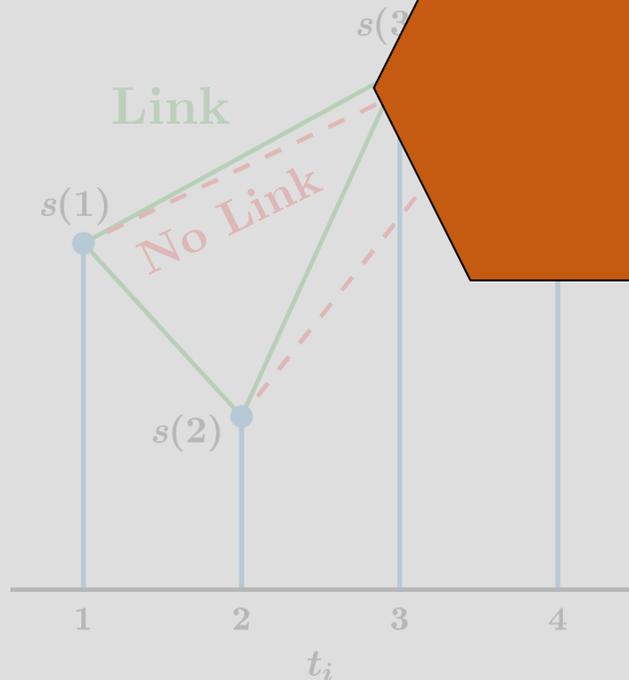




Time series

Mapping
algorithmComplex
Network

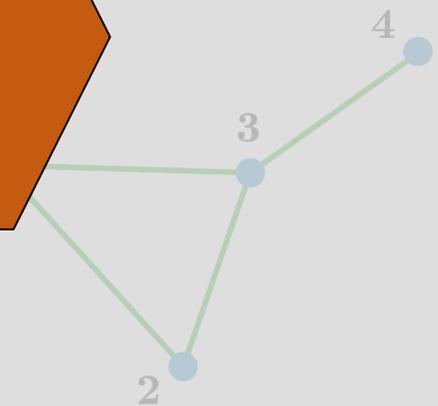
Visibility-networks are
sensitive to the temporal
structure of the series



and translation

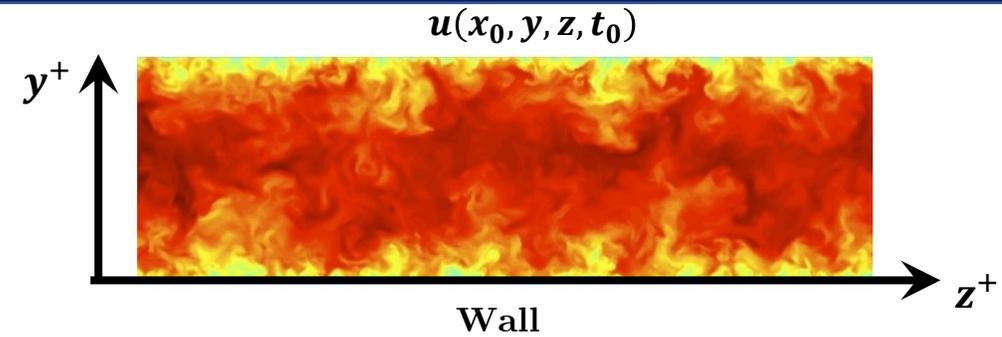
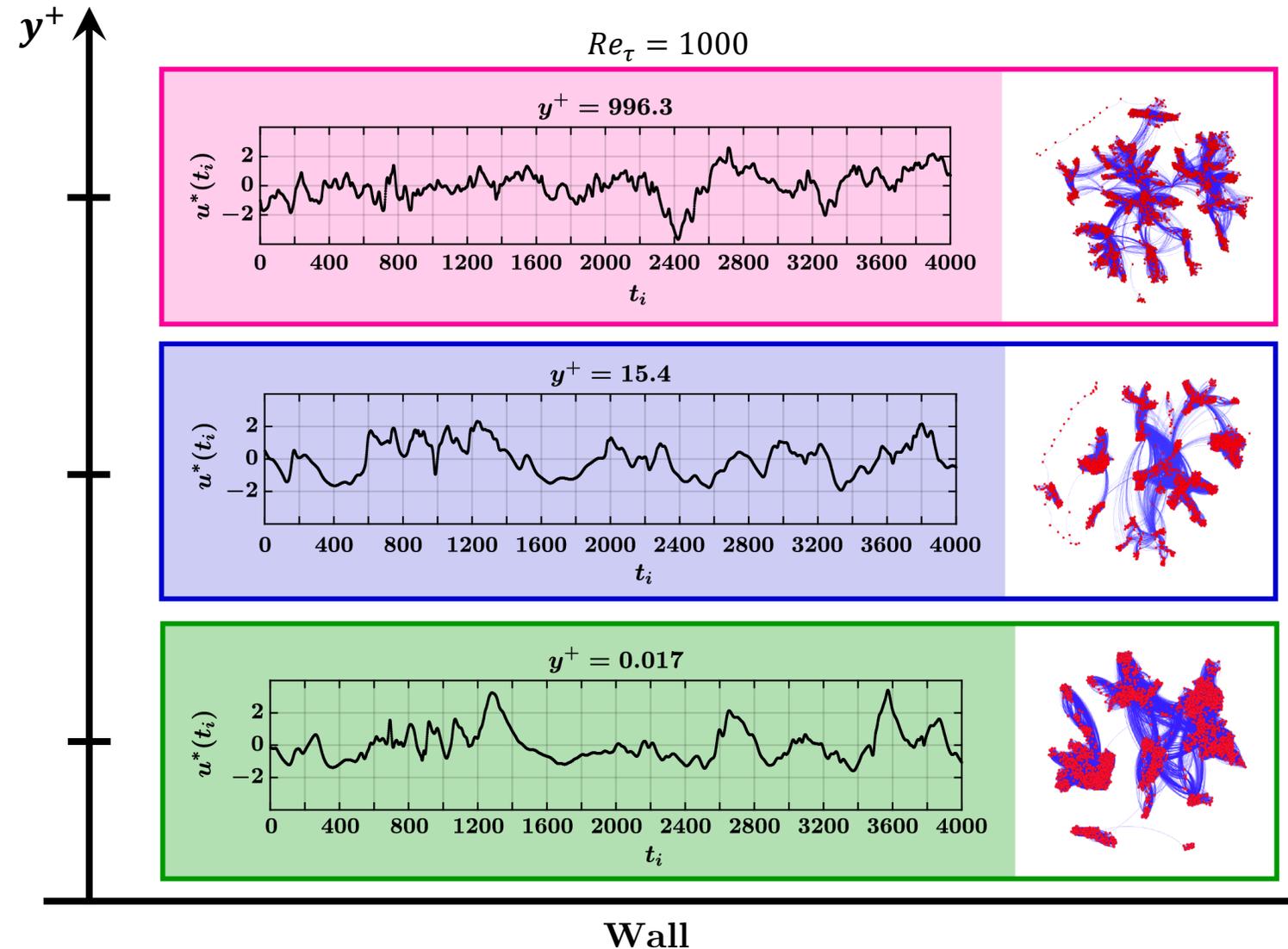
$$s(t_k) < s(t_j) + \left(s(t_i) - s(t_j) \right) \frac{t_k - t_j}{t_i - t_j},$$

$$i < k < j$$



Network hubs \leftrightarrow peaks

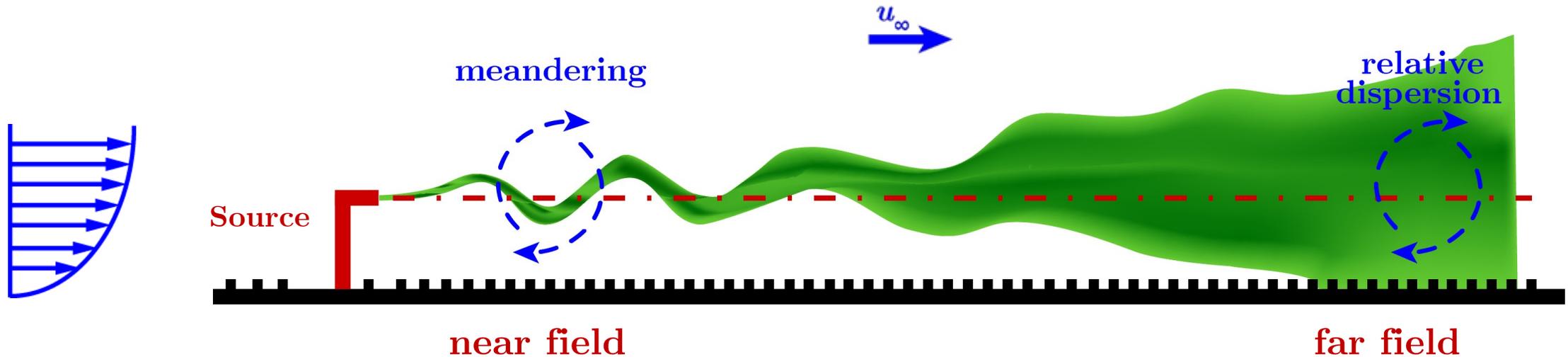
Fully-developed turbulent channel flow (DNS data – Johns Hopkins Turbulence DB)



✓ Different temporal structures →
different network properties

- Highlight **occurrence** of peaks
(extreme events)
- Highlight the presence of **irregularities**
(small fluctuations)
- The **metric behaviours** reveal the relative
intensity of peaks and irregularities

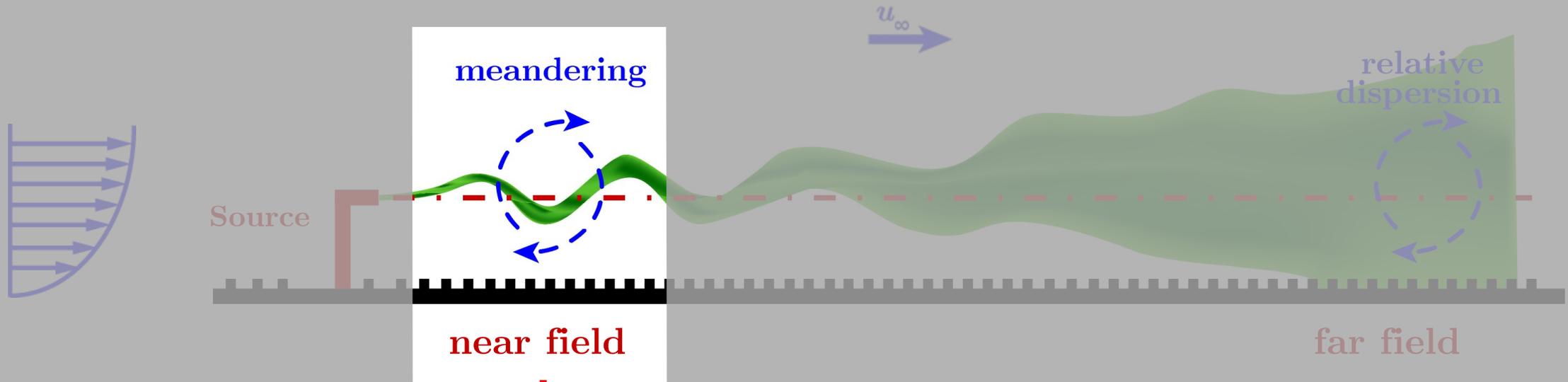
Iacobello, G., Scarsoglio, S., & Ridolfi, L.
(2018). *Physics Letters A*, 382(1), 1-11.

Passive scalar plume in a turbulent boundary layer (experimental data)

Iacobello, G. et al. (2019). *Physical Review Fluids*, 4(10), 104501.

Iacobello, G., et al. (2018). *Progress in Turbulence VIII* (Springer)

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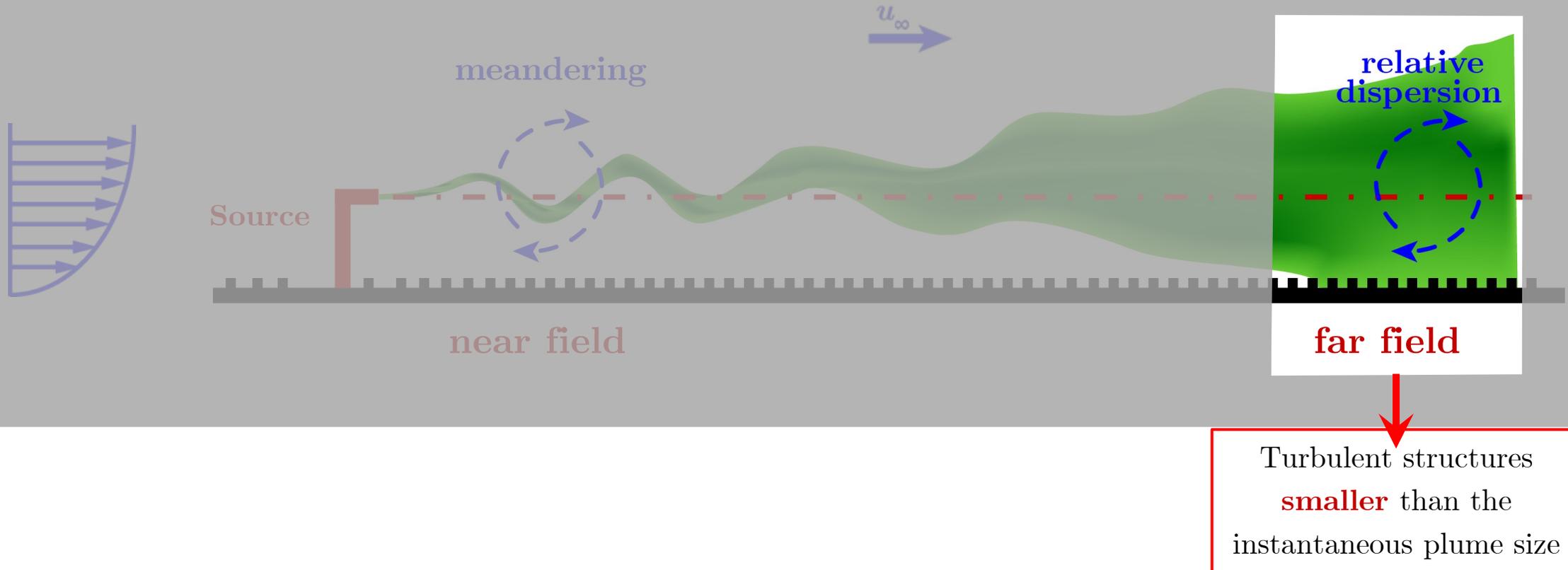


Turbulent structures
larger than the
instantaneous plume size

Iacobello, G. et al. (2019). *Physical Review Fluids*, 4(10), 104501.

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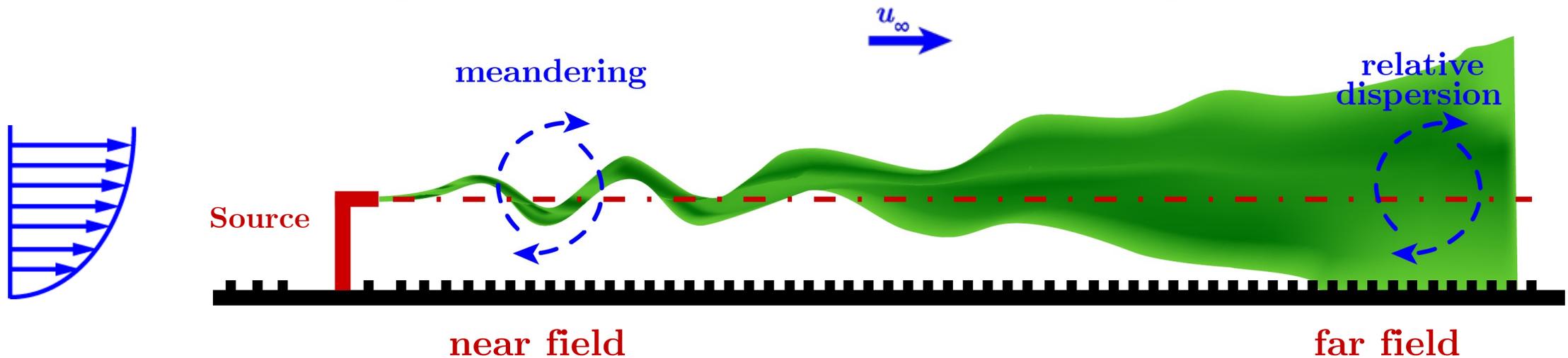
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Passive scalar plume in a turbulent boundary layer (experimental data)



Previous findings:

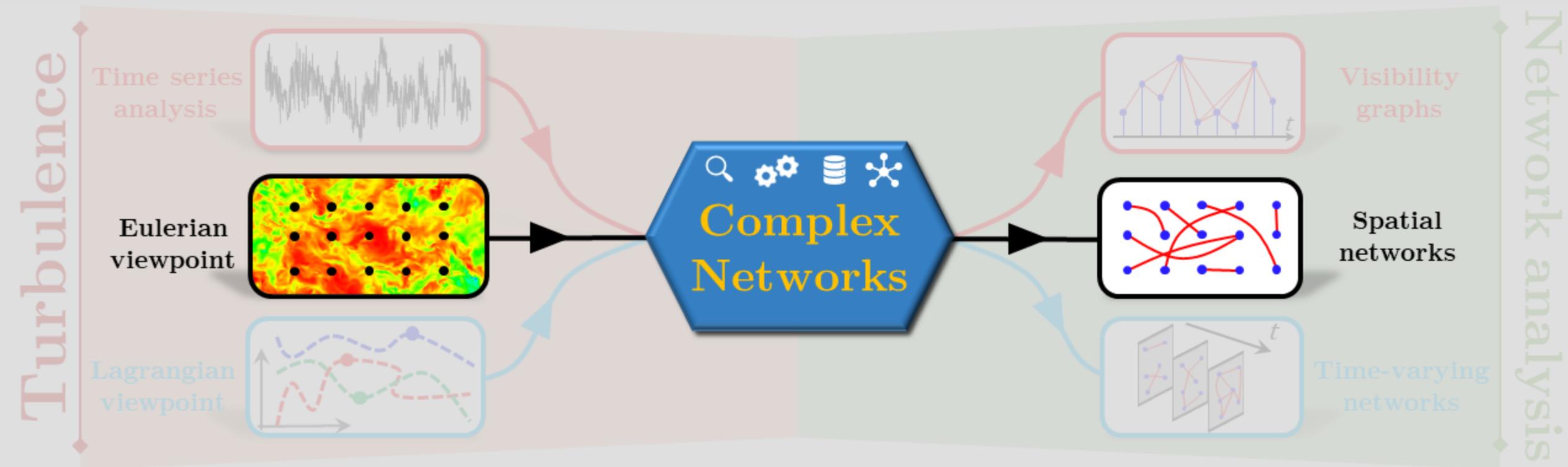
Smaller source size \rightarrow stronger meandering motion (near field) \rightarrow higher intermittency.

Network metrics – Near field:

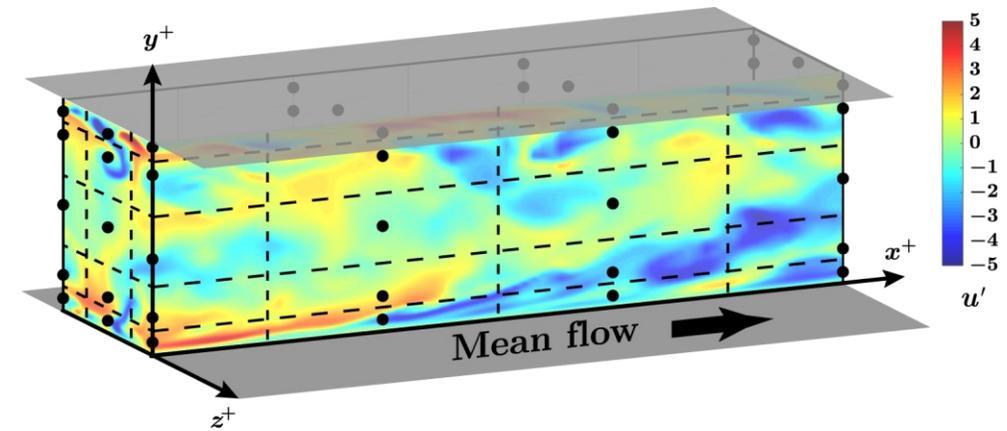
- Decreasing occurrence of extreme events for smaller source sizes;
- Increasing relative intensity of extreme events (outliers) for smaller source sizes.

Iacobello, G. et al. (2019). *Physical Review Fluids*, 4(10), 104501.

Iacobello, G., et al. (2018). *Progress in Turbulence VIII* (Springer)



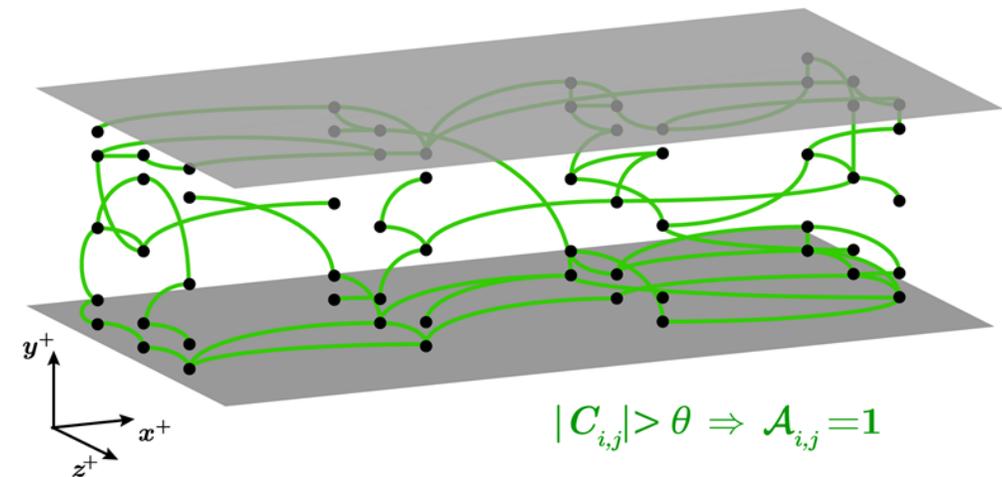
- ❑ DNS of a fully developed **turbulent channel flow**
- ❑ $Re_\tau = 180$
- ❑ Streamwise velocity, u



» What is the spatial organization of high correlation values? «

Spatial correlation-network:

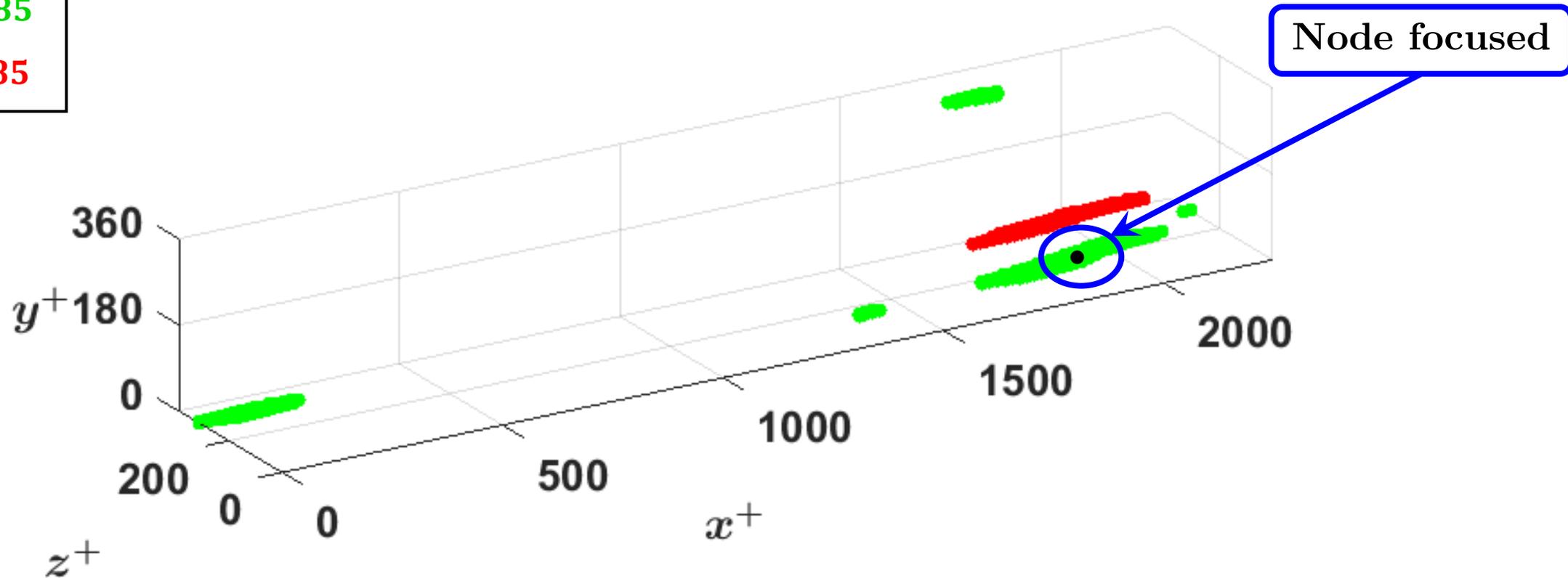
- **Nodes:** fixed spatial positions ($\sim 10^6$)
- **Links:** high u -based correlation coefficients,
 $|C_{i,j}| > threshold$



$$y^+ = 3.5, T^+ = 225$$

$$C_{i,j} > +0.85$$

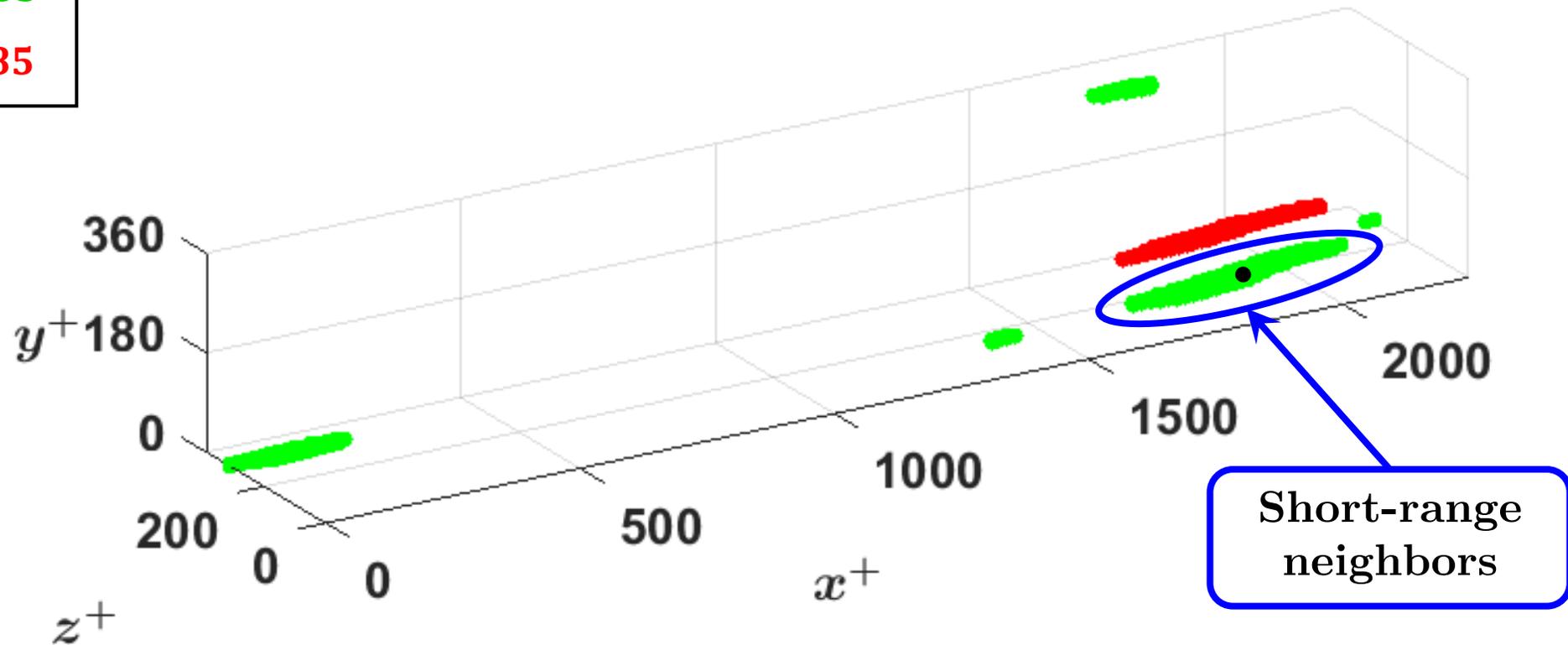
$$C_{i,j} < -0.85$$



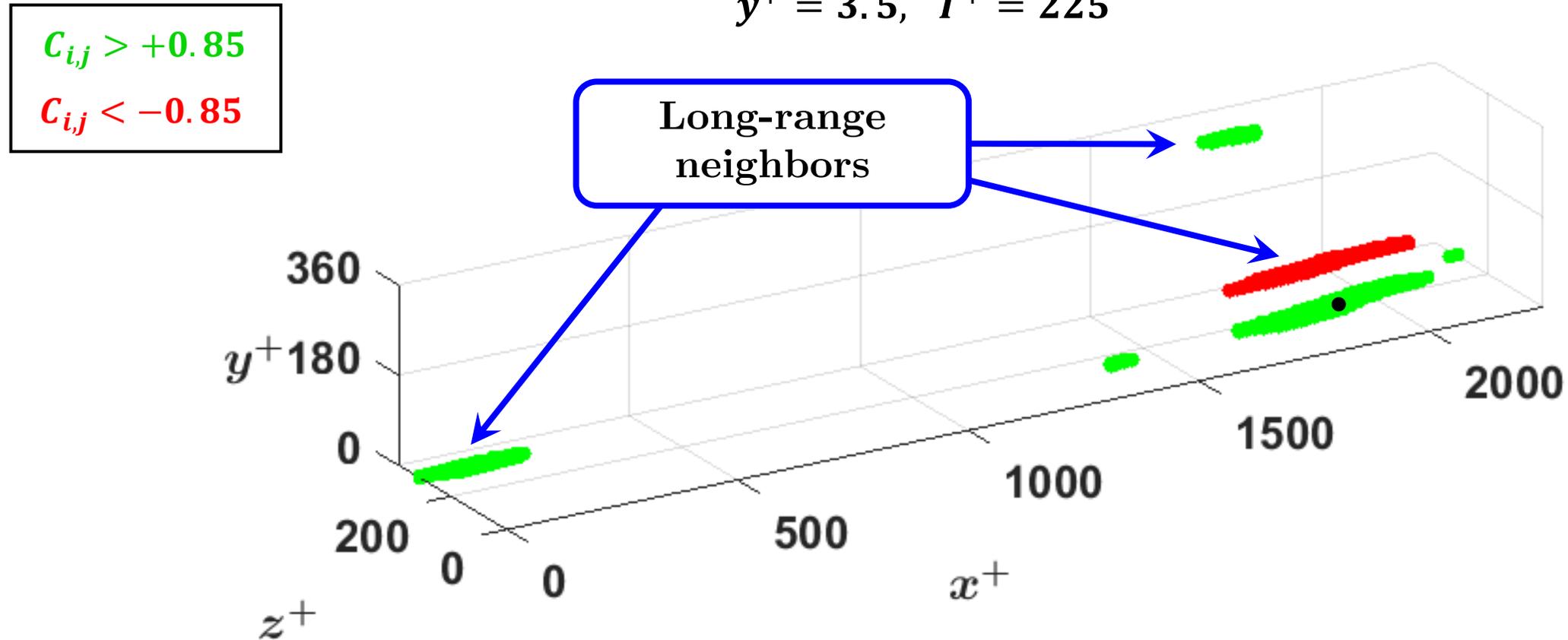
$$y^+ = 3.5, T^+ = 225$$

$$C_{i,j} > +0.85$$

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Short-range
neighbors



Teleconnections:

long-distance high-correlation links →

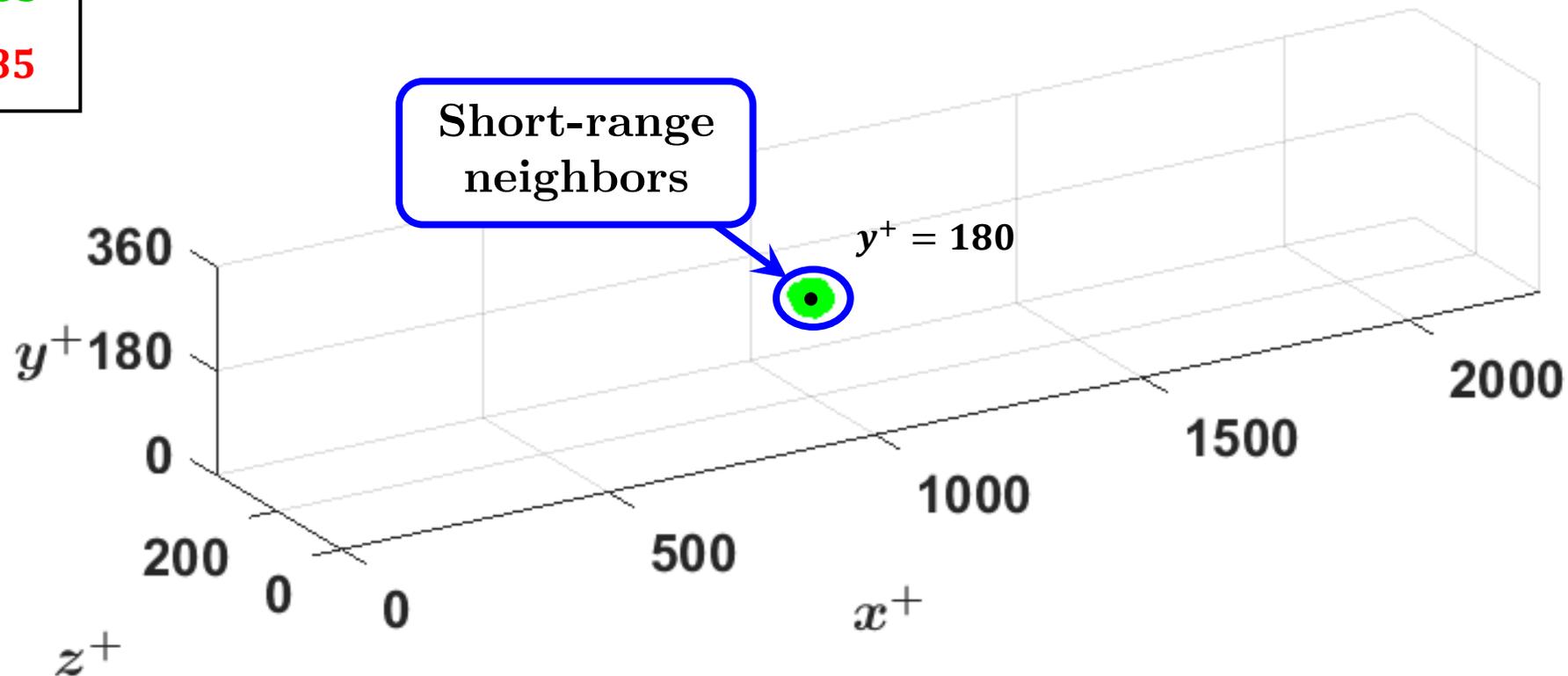
Imprint of coherent high- and low-speed streaks

Iacobello G., Scarsoglio, S., Kuerten, J. G. M., & Ridolfi, L. (2018). *Physical Review E*, 98(1), 013107.

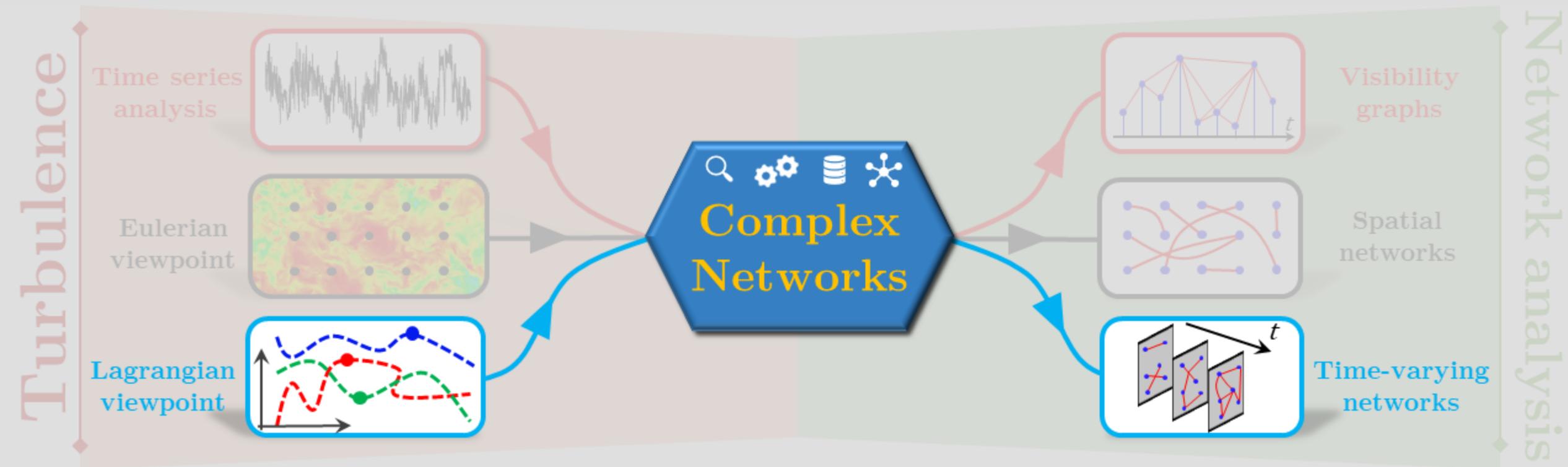
$$y^+ = 180, T^+ = 225$$

$$C_{i,j} > +0.85$$

$$C_{i,j} < -0.85$$



No teleconnections
for nodes far from the walls



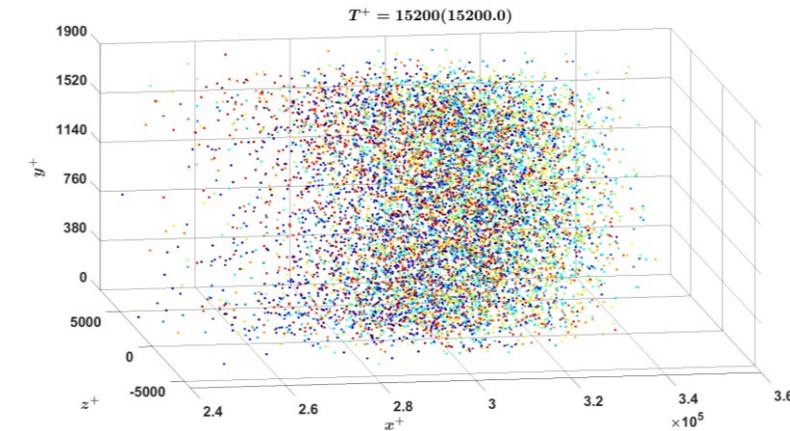
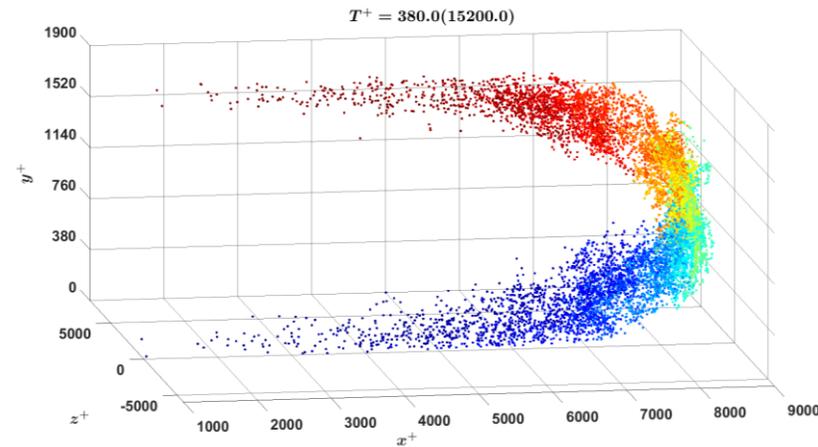
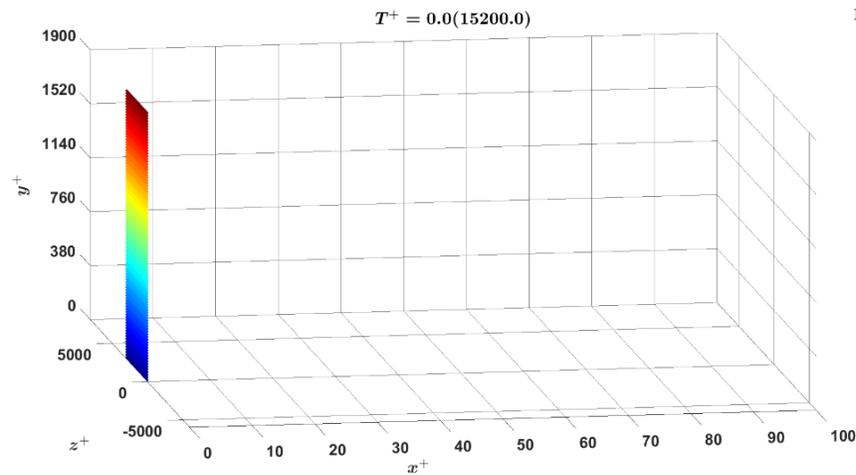
Dispersion of fluid particles in a turbulent channel flow:

DNS:

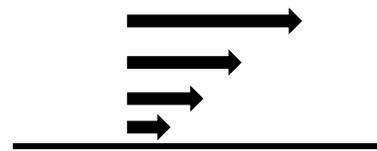
- $Re_\tau = 950$
- $T^+ = 15200$ ($\Delta t^+ = 4.75$)

Fluid particles ($t = 0$):

$$N_y \times N_z = 100 \times 100$$



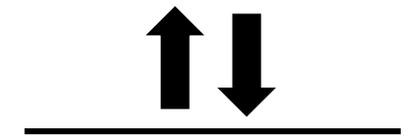
Mean flow
Advection



Short time

+

Wall-normal
Mixing



Long time

t

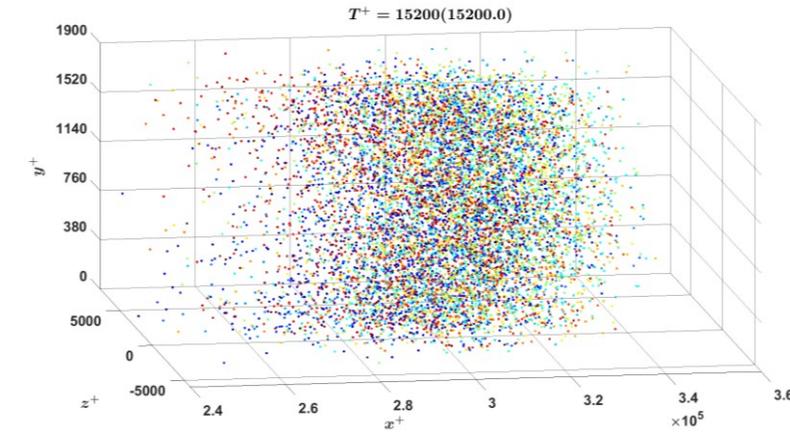
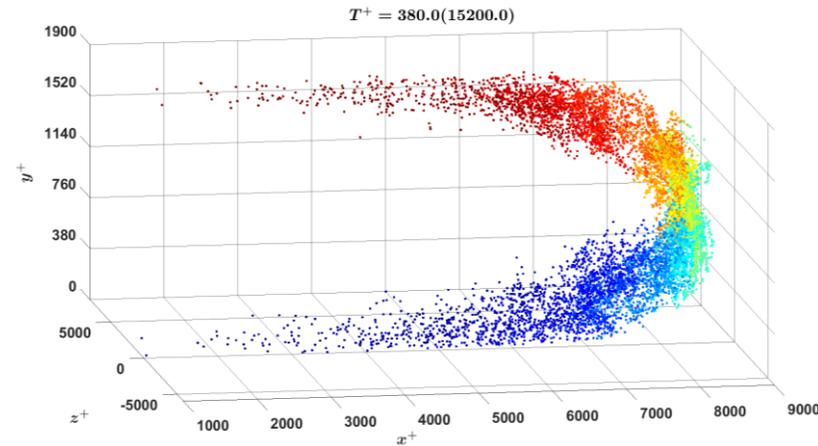
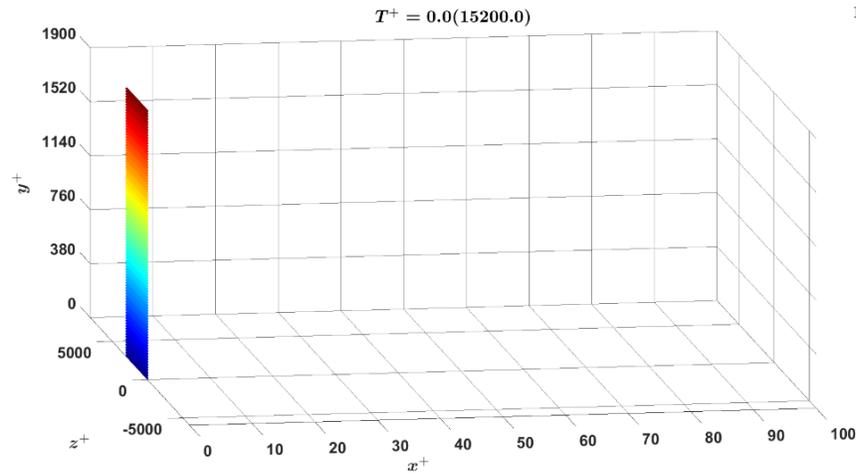
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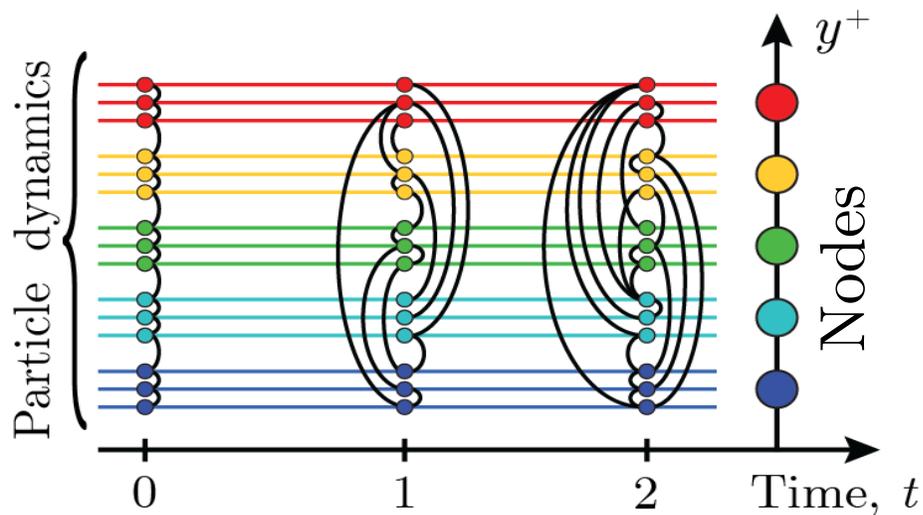
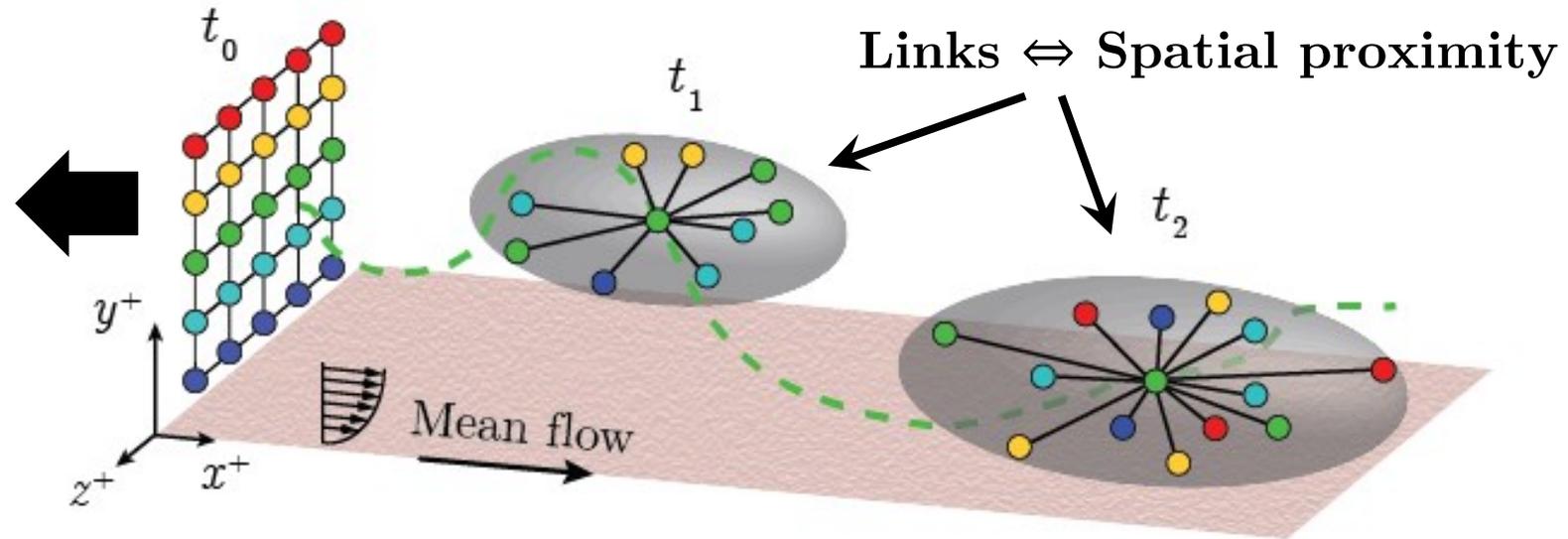


Geometrical representation of turbulence
mixing via complex networks

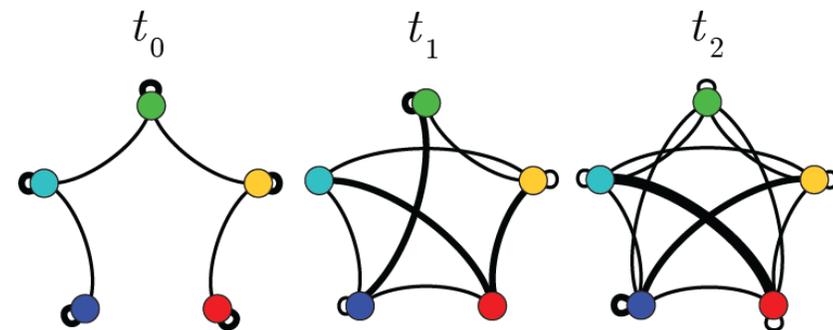
Lagrangian network approach

Iacobello G., Scarsoglio S., Kuerten J.G.M., & Ridolfi L., *Journal of Fluid Mechanics*, 865 (2019), 546-562.

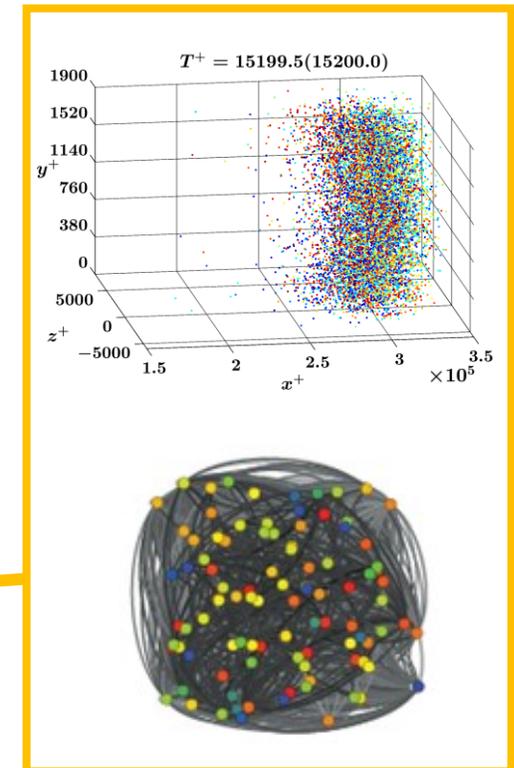
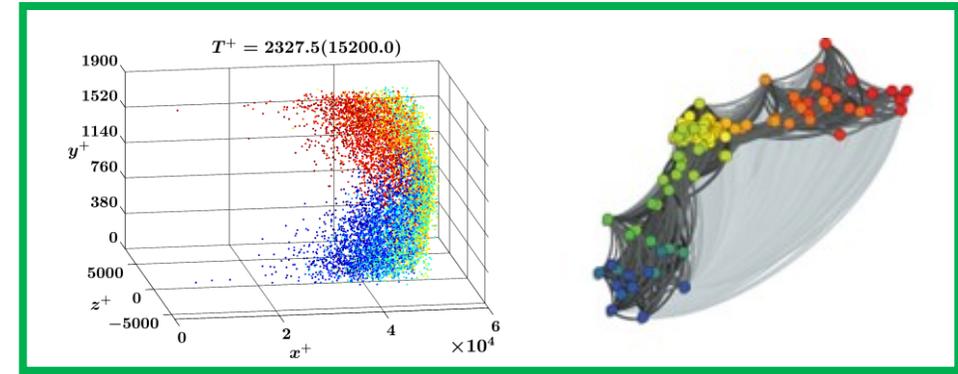
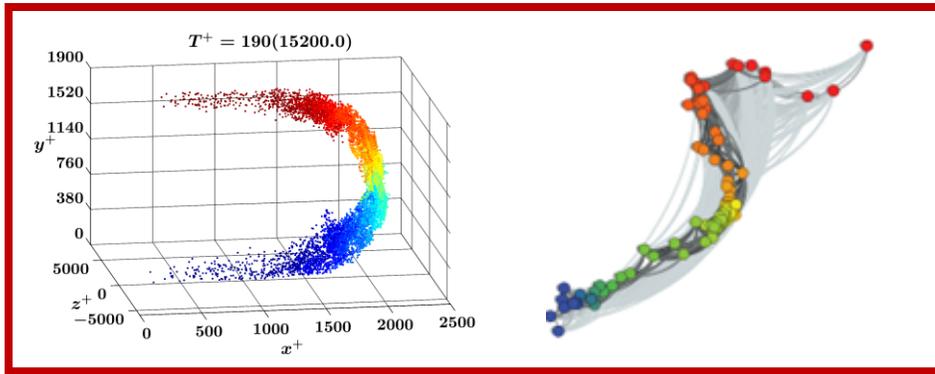
Nodes
= y^+ - rows of particles



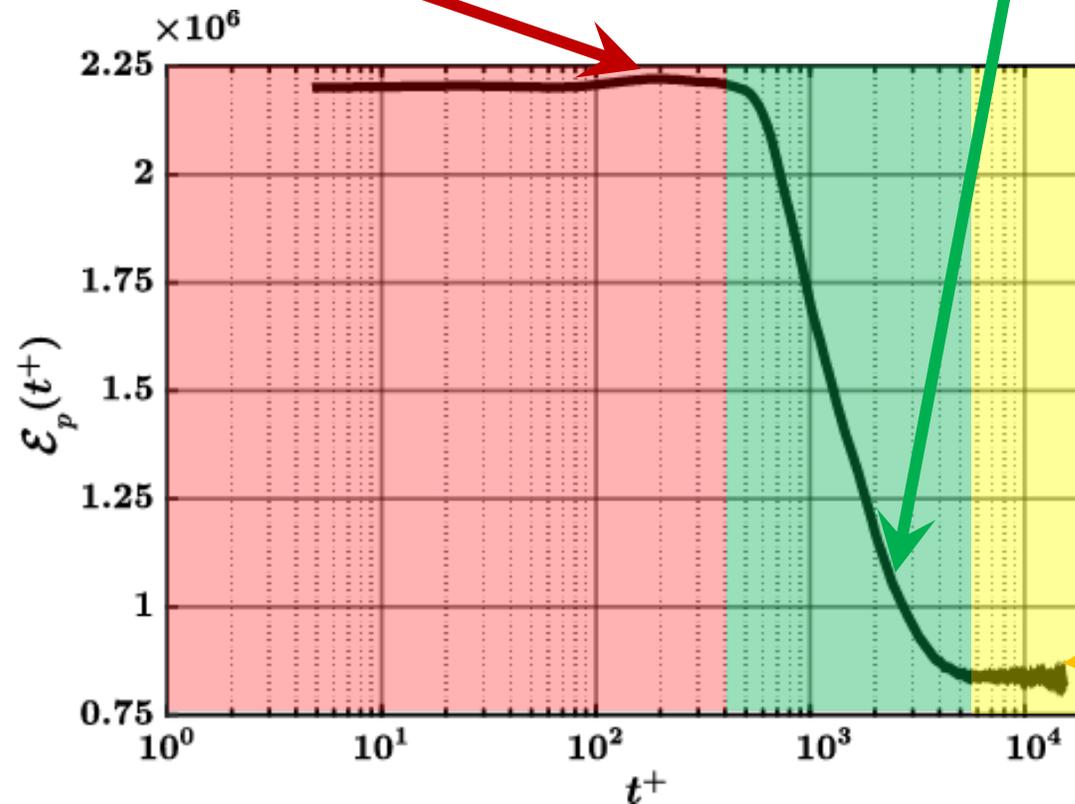
Temporal network evolution



Link weight: number of connections between particles



Total number of connections



Advection regime

Transition regime

Mixing regime

Iacobello G., Scarsoglio S., Kuerten J.G.M., & Ridolfi L., *Journal of Fluid Mechanics*, 865 (2019), 546-562.

✓ Highlight spatio-temporal features of the flow that would be difficult to capture by means of other techniques

• Time-series:

- ❑ Highlight occurrence and (relative) intensity of **extreme events**.
- ❑ Sensitiveness to the **temporal structure** of the signal → Different from kurtosis & higher-order moments

• Spatial networks:

- ❖ Appearance of **teleconnections** between near wall regions along all directions.
- ❖ High-correlation **spatial information** is retained → lost in two-point average correlation.

• Particle trajectory-based networks:

- Identify characteristic regimes of **particle dynamics**: Advection → transition → mixing.
- Lagrangian **transport and mixing** in wall-turbulence.

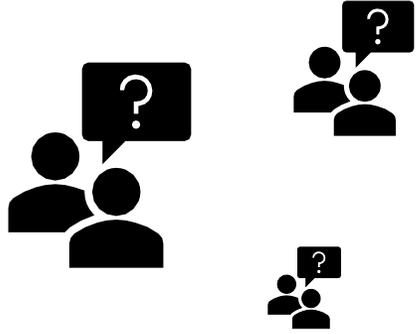
✓ Future outlooks

- **Versatile framework for fluid applications**: inhomogeneous, multiphase flows, biomedical applications

E.g.: **hemodynamics** → see group {L. Ridolfi, S. Scarsoglio, U. Morbiducci} @ Politecnico di Torino

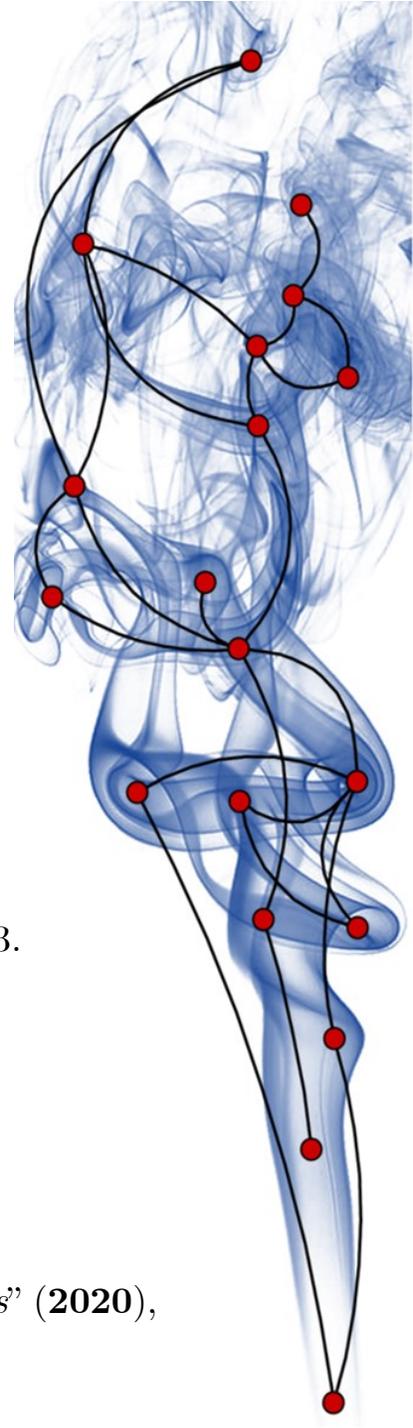
- **Investigate different flow quantities**: velocity, energy, vorticity, ...

- **Higher-order network formulations**: multilayer, simplicial complexes, ...



Thank you for your attention!

Questions?



Contact:

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 www.polito.it/fluidlab/

References:

1. Scarsoglio, S., Iacobello, G., & Ridolfi, L. (2016). **International Journal of Bifurcation and Chaos**, 26(13), 1650223.
2. Iacobello, G., Scarsoglio, S., & Ridolfi, L. (2018). **Physics Letters A**, 382(1), 1-11.
3. Iacobello, G., Scarsoglio, S., Kuerten, J. G. M., & Ridolfi, L. (2018). **Physical Review E**, 98(1), 013107.
4. Iacobello, G., Ridolfi, L., Marro, M., Salizzoni, P., & Scarsoglio, S. (2018). **Progress in Turbulence VIII** (Springer)
5. Iacobello, G., Scarsoglio, S., Kuerten, J. G. M., & Ridolfi, L. (2019). **Journal of Fluid Mechanics**, 865, 546-562.
6. Iacobello, G., Marro, M., Ridolfi, L., Salizzoni, P., & Scarsoglio, S. (2019). **Physical Review Fluids**, 4(10), 104501.
7. Iacobello, G., “*Spatio-temporal analysis of wall-bounded turbulence: A multidisciplinary perspective via complex networks*” (2020), **Doctoral dissertation**, Politecnico di Torino. EMAIL: giovanni.iacobello@polito.it